

Hard Exclusive Meson Electroproduction

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Outline:

- Handbag factorization and GPDs
- Transversely polarized photons matter
- Vector meson production
- Parameterizing GPDs
- Pion production (twist-3, transversity GPDs)
- Summary

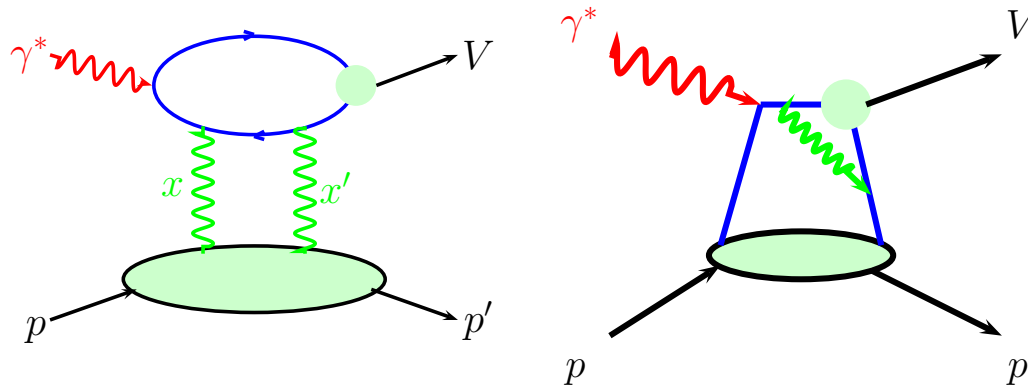
The handbag approach

rigorous proof of collinear factorization for $Q^2 \rightarrow \infty$
(Radyushkin (96); Collins et al (97))

hard subprocesses

$$\gamma^* g \rightarrow V g, \quad \gamma^* q \rightarrow V(P)q$$

and GPDs and meson w.f.
(encode the soft physics)



dominant transition $\gamma_L^* \rightarrow V_L, P$

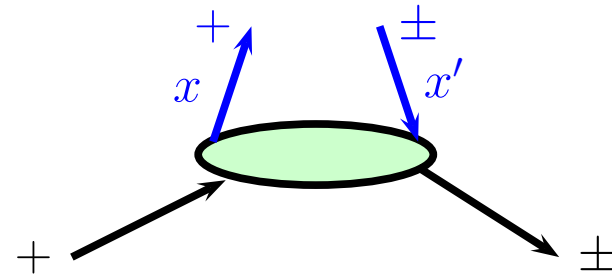
other transitions power suppressed
but often non-negligible (e.g. $\gamma_T^* \rightarrow V_T, \pi$)

GPDs

GPDs: $F = F(\bar{x}, \xi, t)$

$F = H, E, \tilde{H}, \tilde{E}, H_T, \dots$

$$x = \frac{\bar{x} + \xi}{1 + \xi} \quad x' = \frac{\bar{x} - \xi}{1 - \xi}$$



constraints:

Forward limits from DIS: $H^q(\bar{x}, \xi = t = 0) = q(\bar{x})$, $\tilde{H}^q \rightarrow \Delta q(\bar{x})$

$H_T^q \rightarrow \delta^q(\bar{x})$ trans. PDFs, known from SIDIS exp. [Anselmino et al \(07\)](#)

lowest moments (proton form factors): $F_1^q(t) = \int d\bar{x} H^q(\bar{x}, \xi, t)$, $F_1 = \sum e_q F_1^q$
 $E \rightarrow F_2$, $\tilde{H} \rightarrow F_A$

access to parton **angular momentum** (Ji's sum rule)

Fourier transform $\Delta \rightarrow \mathbf{b}$ ($\Delta^2 = -t$): information on parton **localization in transverse position space**

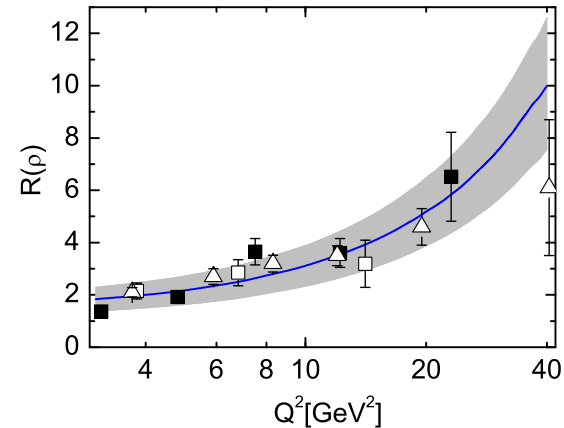
Transverse photon polarization matters

vector-meson electroproduction

$$R = \sigma_L / \sigma_T \quad (\text{HERA } W \simeq 80 \text{ GeV})$$

$\gamma_T^* \rightarrow V_T$ transitions substantial

power corr. and/or higher twist needed



various moments of π^+ cross section

measured with trans. pol. target

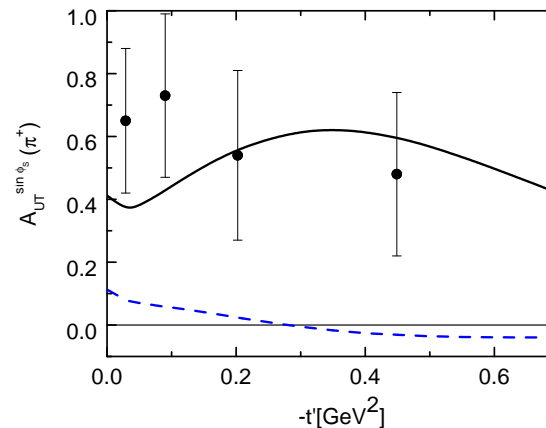
$\sin \phi_s$ moment very large

does not seem to vanish for $t' \rightarrow 0$

$$A_{UT}^{\sin \phi_s} \propto \text{Im} \mathcal{M}_{0+,0+}^* \mathcal{M}_{0-,++}$$

requires n-f. ampl. $\mathcal{M}_{0-,++}$

$\gamma_T^* \rightarrow P$ transitions substantial



HERMES

$$Q^2 \simeq 2.5 \text{ GeV}^2, \quad W = 3.99 \text{ GeV}$$

The $\gamma^* p \rightarrow VB$ amplitudes

consider large Q^2 , W and small t ;

kinematics fixes skewness: $\xi \simeq \frac{x_{Bj}}{2-x_{Bj}} [1 + m_V^2/Q^2] \simeq x_{Bj}/2 + \text{m.m.c.}$

$$\mathcal{M}_{\mu+, \mu+}(V) = \frac{e_0}{2} \left\{ \sum_a e_a \mathcal{C}_V^{aa} \langle H_{\text{eff}}^g \rangle_{V\mu} + \sum_{ab} \mathcal{C}_V^{ab} \langle H_{\text{eff}}^{ab} \rangle_{V\mu} \right\},$$

$$\mathcal{M}_{\mu-, \mu+}(V) = -\frac{e_0}{2} \frac{\sqrt{-t'}}{M+m} \left\{ \sum_a e_a \mathcal{C}_V^{aa} \langle E^g \rangle_{V\mu} + \sum_{ab} \mathcal{C}_V^{ab} \langle E^{ab} \rangle_{V\mu} \right\},$$

\mathcal{C}_V^{ab} flavor factors, $M(m)$ mass of $B(p)$, $H_{\text{eff}} = H - \xi^2/(1 - \xi^2)E$

$$F^{aa} = F^a \quad F^{ab} = F^a - F^b \quad (a \neq b)$$

$$\langle F \rangle_{V\mu} = \sum_\lambda \int_{-1}^1 d\bar{x} \mathcal{H}_{\mu\lambda, \mu\lambda}^V(\bar{x}, \xi, Q^2, t=0) F(\bar{x}, \xi, t)$$

electroproduction with unpolarized protons at small ξ :

E not much larger than H (see below) $\implies H_{\text{eff}} \rightarrow H$ for small ξ

$|M_{\mu-, \mu+}|^2 \propto t/m^2$ **neglected** \implies **probes H** (exception ρ^+)

trans. polarized target: probes $Im[\langle E \rangle^* \langle H \rangle]$ interference

What did (can) we learn about GPDs from DME?

What is probed by exp.: **imag. parts** \propto GPDs at $\xi \simeq \bar{x} + \mathcal{O}(\langle k_{\perp}^2 \rangle / Q^2)$
real parts - convolutions, dominated by \bar{x} near ξ

$\xi \simeq 10^{-3}$ **HERA**

$\simeq 10^{-2}$ **COMPASS**

$\simeq 10^{-1}$ **HERMES**

$\simeq 0.1 - 0.4$ **JLab**

$\bar{x} \geq 0.6$ not probed

large \bar{x} region important

LO, lead.twist accuracy (Teryaev (05)) e.g.:

$$\langle F \rangle = c \int_{-1}^1 d\bar{x} \left[\frac{1}{\bar{x} - \xi + i\epsilon} + \frac{1}{\bar{x} + \xi - i\epsilon} \right] F(\bar{x}, \xi, t)$$

$$\text{Im}\langle F \rangle \sim F(\xi, \xi, t), \quad \text{Re}\langle F \rangle = cPV \int_0^1 d\bar{x} \frac{2\bar{x}^2}{\xi^2 - \bar{x}^2} F(\bar{x}, \bar{x}, t)$$

As compared to DVCS:

disadvantage: need for GPDs and meson wave functions

advantages: allows for flavor separation (mesons select their valence quarks

J/Ψ : gluon from the proton to lead. twist accuracy)

ϕ : gluon + sea

ρ^0, ω : gluon + sea + valence

ρ^+, π^+ : valence

mainly H

π^+ : \tilde{H}, \tilde{E}

Parameterizing the GPDs

double distribution ansatz (Mueller *et al* (94), Radyushkin (99))

$$F_i(\bar{x}, \xi, t') = \int_{-1}^1 d\beta \int_{-1+|\beta|}^{1-|\beta|} d\alpha \delta(\beta + \xi\alpha - \bar{x}) f_i(\beta, \alpha, t') + D_i \Theta(\xi^2 - \bar{x}^2)$$

DD: f_i = zero-skewness GPD \times weight fct (generating ξ dep.)

$$F(\bar{x}, \xi = 0, t) = f(\bar{x}) \exp [(b_f + \alpha'_f \ln(1/\bar{x}))t]$$

$$f = q, \Delta q, \delta^q \text{ for } H, \tilde{H}, H_T \text{ or } c\bar{x}^{-\alpha_f(0)}(1 - \bar{x})^{\beta_f}$$

Regge-like t dep. large x , large $-t$ more complicated profile fct Diehl *et al* (04)

advantage: polynomiality and reduction formulas automatically satisfied

dual parameterization (Polyakov(99), Polyakov-Semenov(09))

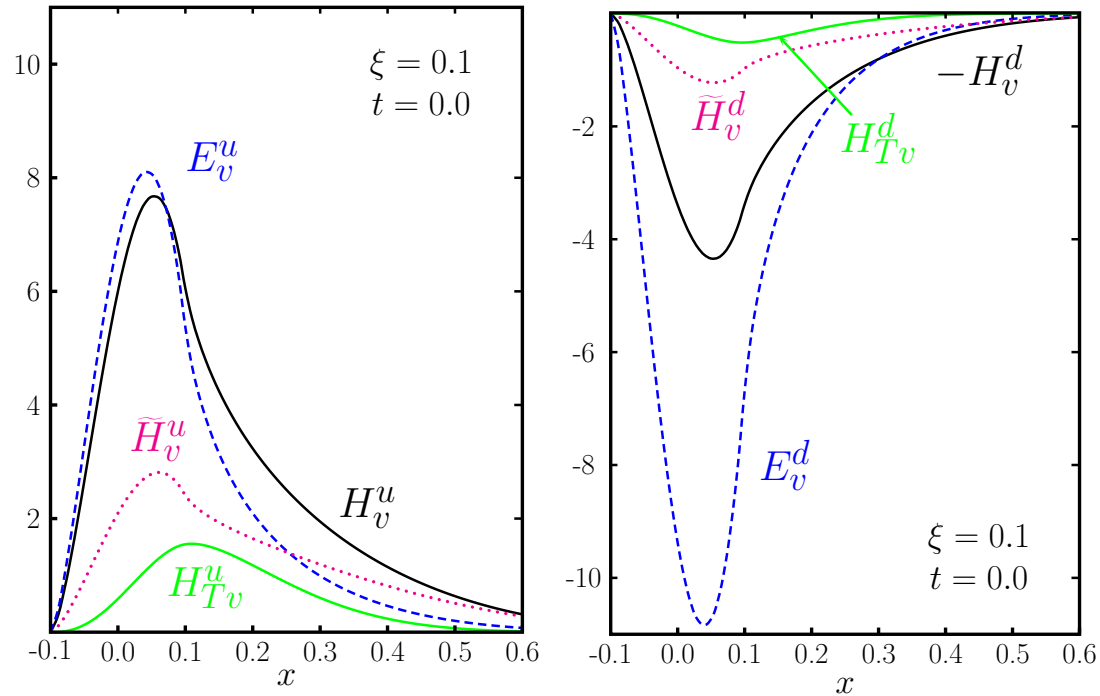
repres. of GPDs in terms of infinite sum of t -channel resonances - 'duality'

in practice: truncation of partial wave series at small j

e.g. Bechler-Mueller(09) for π^+ production:

zero-skewness GPD (as above) and rot. matrices $d_{0,m}^{j+m}(1/\xi)$

Valence quark GPDs



satisfy:

- polynomiality
- PDFs (if available)
- nucleon form factors
- positivity bounds

scale: 4GeV^2

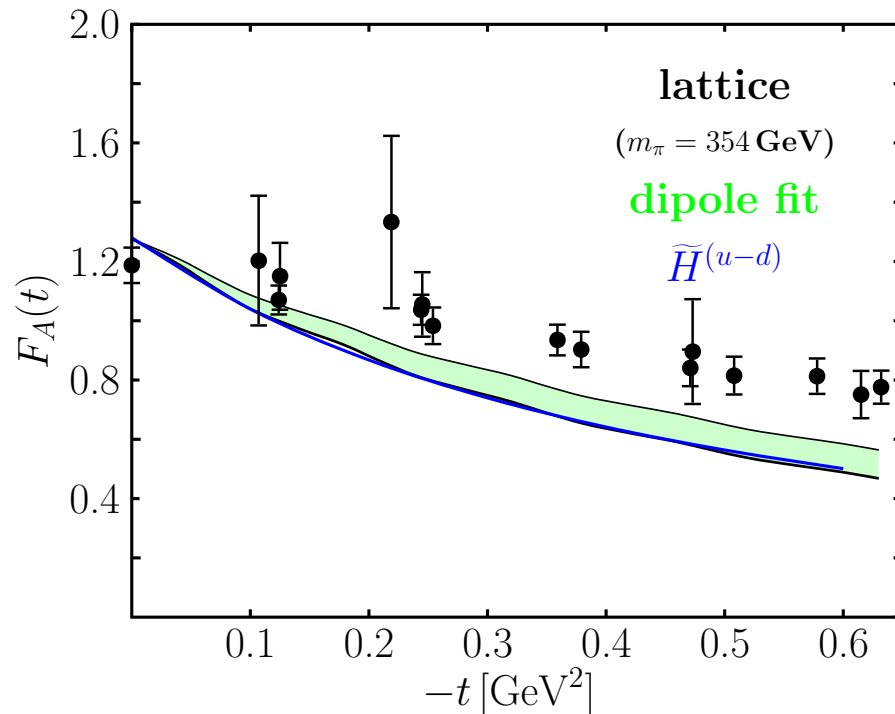
	H	E	\tilde{H}
u_v	2	$\kappa_u = 1.67$	0.93
d_v	1	$\kappa_d = -2.03$	-0.34

lowest moments

fix signs and rel. sizes

if GPDs have no nodes and similar t dependence

Comparison with lattice results



Hägler (07), Gökeler (05)

lowest pion mass 352 MeV
no chiral extrapolation

exceptions:

2nd moments of H and E

\implies Ji's sum rule (see below)

Relative sizes of the moments and relative t dependence in reasonable agreement with DD ansatz

in general t dependences flatter than DD ansatz (and form factor data)

H_T lattice moments are larger by about factor of 2 as those constructed from transversity PDFs with help of DD ansatz

Numerical results for vector mesons

Goloskokov-K. 06, 07, 08, 09

subprocess amplitudes: mod. pert. approach (Serman et al (93))

LO pQCD+ quark trans. mom. + Sudakov suppr. \Rightarrow lead. twist for $Q^2 \rightarrow \infty$

GPDs constructed from CTEQ6 PDFs through the double distr. ansatz

Gaussian wave fcts for the mesons $\Psi_{Vj}(\tau, \mathbf{k}_\perp) \propto \exp[-a_{Vj}^2 \mathbf{k}_\perp^2 / (\tau \bar{\tau})]$

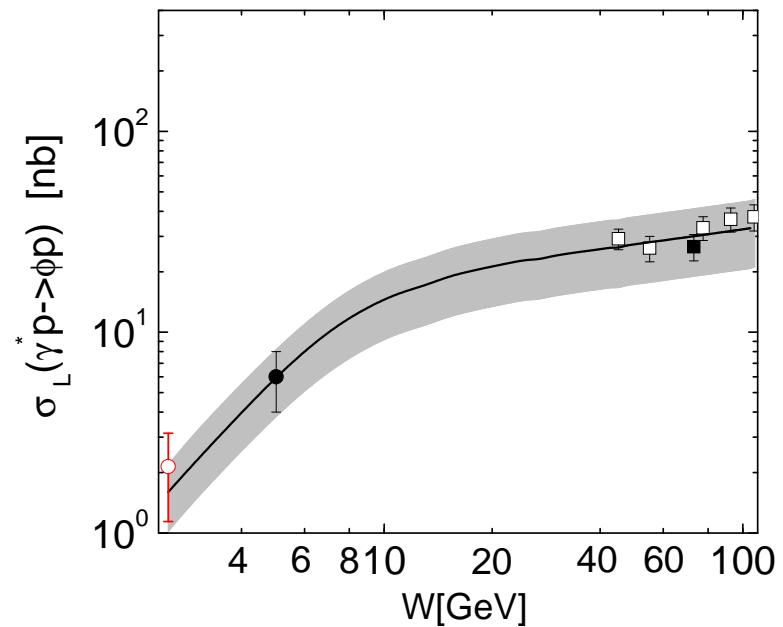
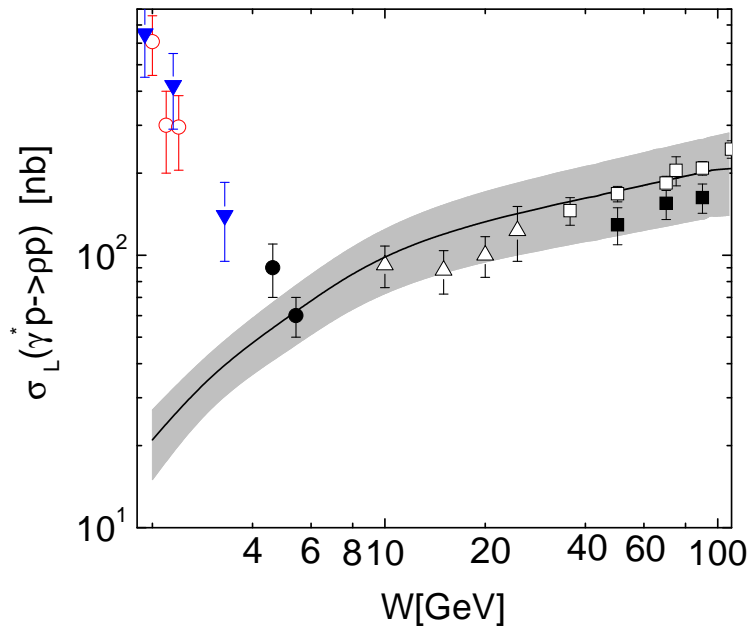
L and T different, free parameters - $a_{L,T}^V$ (transverse size $\langle k_\perp^2 \rangle^{1/2} \propto 1/a_{L,T}^V$)

fit to all data from HERMES, COMPASS, E665, H1, ZEUS

cover large range of kinematics $Q^2 \simeq 3 - 100 \text{ GeV}^2$ $W \simeq 5 - 180 \text{ GeV}$

probes H

ρ^0 and ϕ cross sections



at $Q^2 = 4(3.8) \text{ GeV}^2$ E665 (Δ), HERMES (\bullet), CORNELL (\blacktriangle)
 ZEUS (\square), H1 (\blacksquare), CLAS (\circ)

Goloskokov-K (09)

double distribution ansatz too simple for valence quarks for large ξ ?

breakdown of handbag physics?

ω , ρ^+ very large at small W too CLAS

JLAB12 may explore region close to minimum

What do we know about E_v ?

analysis of Pauli FF for proton and neutron at $\xi = 0$ Diehl et al (04):

$$F_2^{p(n)} = e_{u(d)} \int_0^1 dx E_v^u(x, \xi = 0, t) + e_{d(u)} \int_0^1 dx E_v^d(x, \xi = 0, t)$$

ansatz for small $-t$: $E_v^a = e_v^a(x) \exp \left\{ t(\alpha'_v \ln(1/x) + b_a^e) \right\}$

forward limit: $e_v^a = N_a x^{-\alpha_v(0)} (1-x)^{\beta_v^a}$ (analogously to PDFs)

N_a fixed from $\kappa_a = \int_0^1 dx E_v^a(x, \xi = 0, t = 0)$

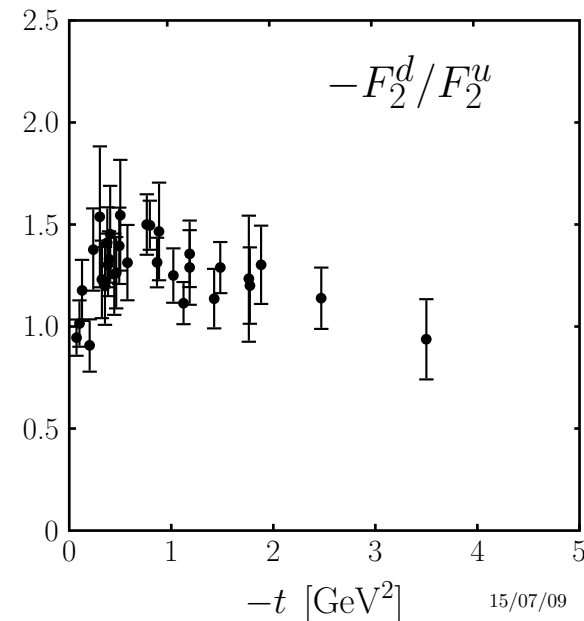
fitting FF data provides: $\beta_v^u = 4, \beta_v^d = 5.6$

(other powers not excluded in 04 analysis)

new JLab data on $G_{E,M}^n$

up to 3.5(5.0) GeV^2 favor $\beta_v^u < \beta_v^d$

Input to double distribution model



E for gluons and sea quarks

sum rule (Ji's s.r. and momentum s.r. of DIS) at $t = \xi = 0$

$$\int_0^1 dx x e_g(x) = e_{20}^g = - \sum e_{20}^{a_v} - 2 \sum e_{20}^{\bar{a}}$$

valence term very small, in particular if $\beta_v^u \leq \beta_v^d$

\Rightarrow gluon and sea quark moments cancel each other almost completely

positivity bound forbids large sea \Rightarrow gluon small too

Simplest variant (1): neglect E^g, E^{sea} (other variants also used)

Ji's sum rule (at scale 4 GeV^2):

$$J^u = 0.250 \quad J^d = 0.020 \quad J^s = 0.015 \quad J^g = 0.214 \quad \sum J^i \simeq 1/2$$

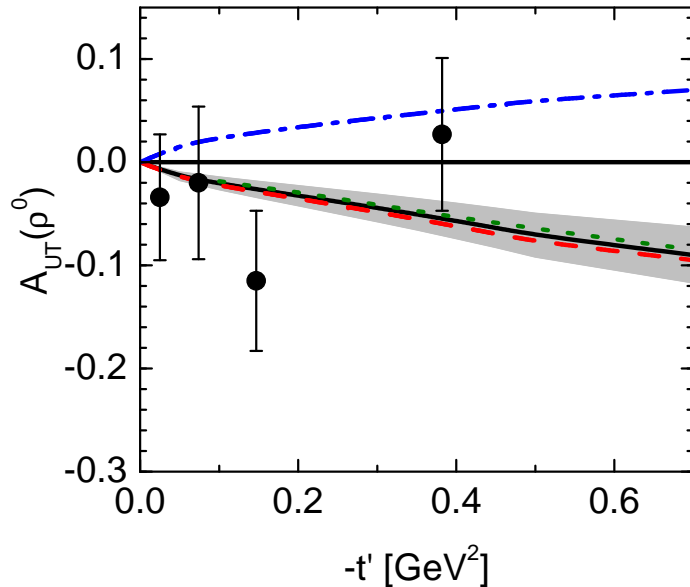
$$\implies J^{u_v} = 0.211(17) \quad J^{d_v} = 0.000(19) \quad (\text{Diehl et al (04)})$$

lattice Hägler et al (07) at $m_\pi(\text{phys})$: $J^u = 0.214(27) \quad J^d = -0.001(27)$

sea quark contr. seems to be small

Results for $A_{UT}(V)$

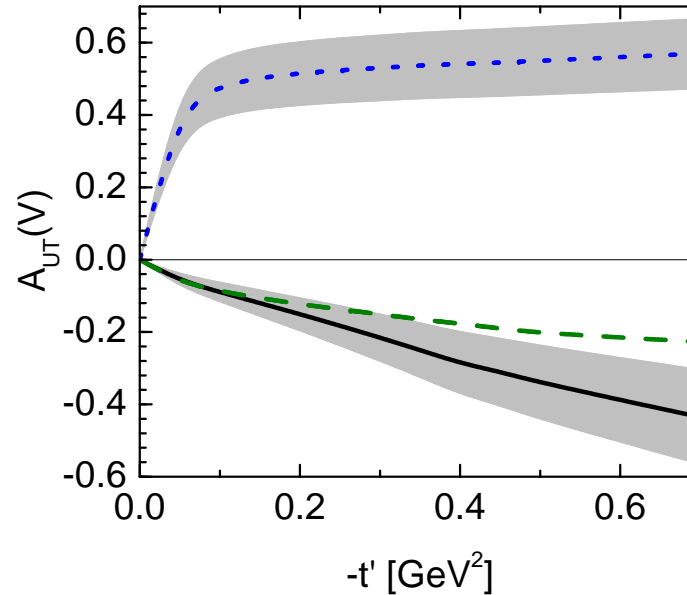
Goloskokov-K (08)



$W = 5 \text{ GeV}$ $Q^2 = 3 \text{ GeV}^2$

variant 1, 2, 3, 4

preliminary data: HERMES (07)



variant 1 for ω , ρ^+ , K^{*0}

t dependence controlled by trivial factor $\sqrt{-t'}$

except for ρ^+ : since $H_v^u - H_v^d$ small and $E_v^u - E_v^d$ large

E non-negligible in cross section, contribution from helicity flip ampl. $\propto t'$

more data on ρ^0, ω, ϕ from HERMES and COMPASS will come

Exclusive electroproduction of pions

as for vector-mesons with replacement $H \Rightarrow \tilde{H}$ and $E \Rightarrow \tilde{E}$

for π^+ production: only $\tilde{H}^{(3)} = \tilde{H}_v^u - \tilde{H}_v^d$ and $\tilde{E}^{(3)} = \tilde{E}_v^u - \tilde{E}_v^d$
(including the pion pole)

for π^0 production: $e_u \tilde{H}_v^u - e_d \tilde{H}_v^d$ and $e_u \tilde{E}_v^u - e_d \tilde{E}_v^d$ (without pion pole)

JLab kinematics: π^0 cross section underestimated by handbag appr (as for ρ^0)?

full pion FF needed and extra \tilde{E} see Goloskokov-K(09), Bechler-Müller (09)

Bechler-Müller (09): leading-twist analyses with $\alpha_s^{\text{eff}} = 0.8$, only LL ampl.

Goloskokov-K(09): plus twist-3 effect for LT ampl. (transversity GPDs)

Ahmad et al (08): only π^0 production with contr. from transversity GPDs

A twist-3 contribution

$$A_{UT}^{\sin \phi_s} \sim \text{Im} [\mathcal{M}_{0-++}^* \mathcal{M}_{0+0+}]$$

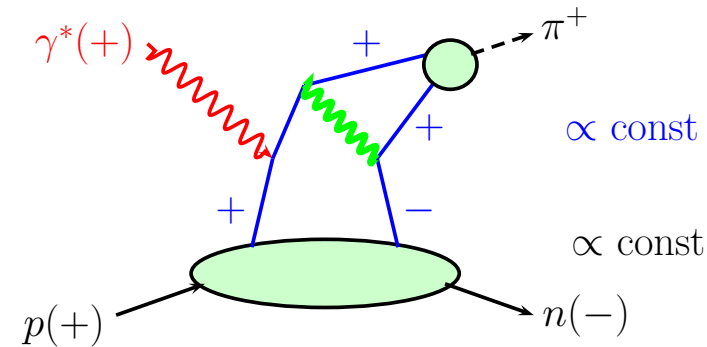
\mathcal{M}_{0-++} fed by handbag dynamics

but with transversity GPDs

(Hoodbhoy-Ji (98), Diehl (01))

and twist-3 pion wave fct

$$\mathcal{M}_{0-++} \sim \langle H_T \rangle$$



twist-3 pion DA: $\langle \pi^+(q') | \bar{d}(x) \gamma_5 u(-x) | 0 \rangle = f_\pi \mu_\pi \int d\tau e^{q' \cdot x \tau} \Phi_P(\tau)$

local limit $x \rightarrow 0$ related to divergency of axial-vector current

$$\Rightarrow \mu_\pi = m_\pi^2 / (m_u + m_d) \simeq 2 \text{ GeV at scale } 2 \text{ GeV}$$

twist-3 large, only suppressed by μ_π / Q

$$\Phi_P = 1 \text{ (under neglect of } q\bar{q}g \text{ Fock state)}$$

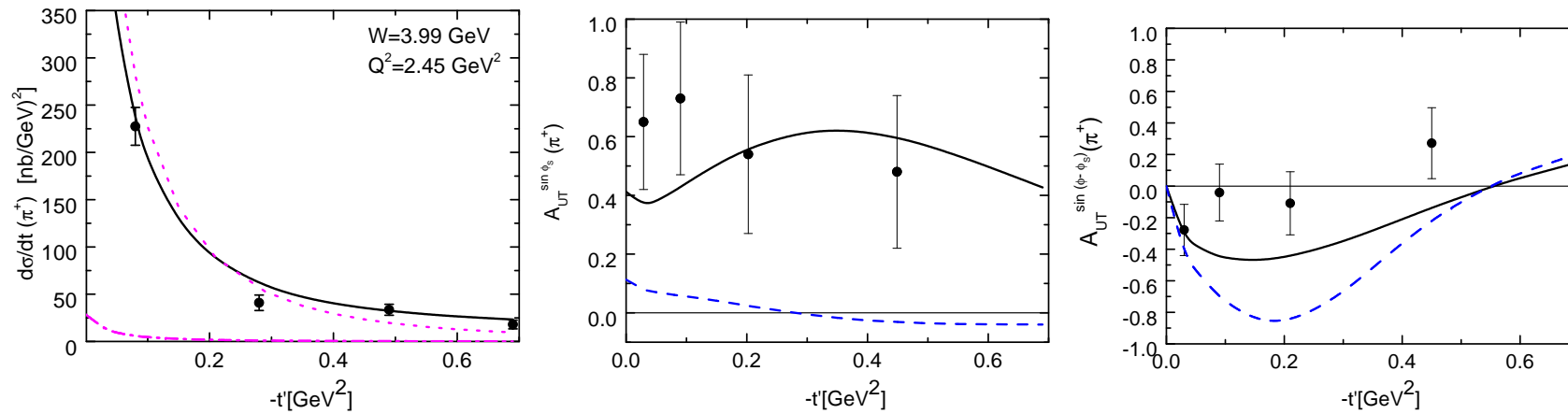
Braun-Halperin (90)

small ξ : H_T should dominate; take transversity PDF from Anselmino et al (07)

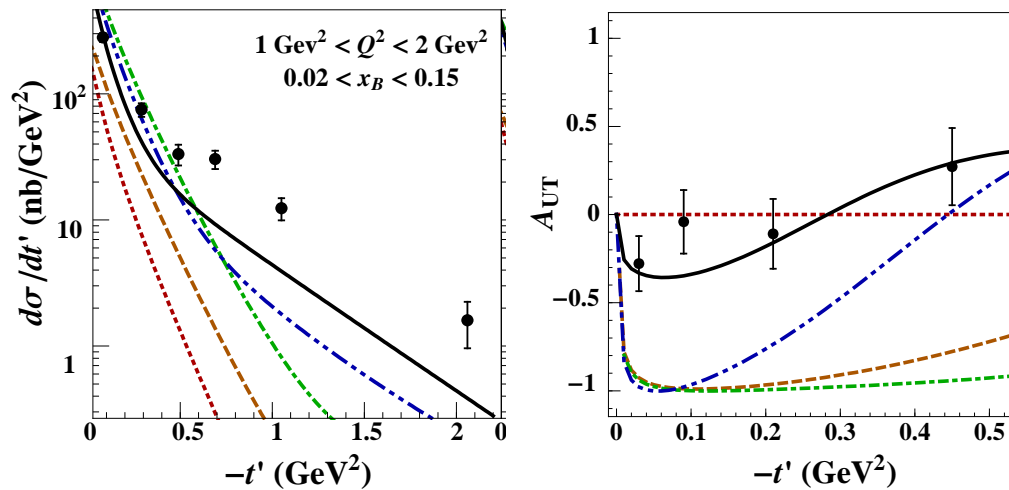
$$\delta^a = 7.46 N_T^a (1-x)^5 [q(x) + \Delta q(x)] \quad N_T^u = 0.5 \quad N_T^d = -0.6$$

input to double distr. ansatz

Results on π^+ production



Goloskokov-K (09) $Q^2 = 2.5$ GeV² $W = 3.99$ GeV
 data HERMES (07)(08)



Bechler-Müller (09)
 only LL amplitudes
 (black lines)

Summary

- handbag approach: fair agreement with cross section data for vector mesons at small ξ has been found
GPDs (H) modeled through reggeized double distributions and subprocess calculated within mod. pert. approach
few free parameters (a_V)
extension to large ξ (JLab kinematics) seems to be difficult
- single spin asymmetries will fix E ; probably dominated by valence quarks;
 E^g and E^{sea} probably small
- first attempts to understand π^+ electroproduction
required are GPDs \tilde{H} and \tilde{E} , pion exchange and a twist-3 effect for transversely pol. photons
(e.g. helicity-flip GPD H_T and twist-3 pion wave fct.)